

## 402(4): The Vacuum Fluctuation Responsible for the Relativistic Newton Equation

The relativistic Newton equation is:

$$\underline{F} = \gamma^3 m \underline{\ddot{r}} = -nMG \frac{\underline{r}}{r^3} \quad (1)$$

where

$$\gamma^3 = \left(1 - \frac{v^2}{c^2}\right)^{-3/2} \quad (2)$$

IN E(2) theory:

$$\underline{F} = -\underline{\nabla} \phi + \underline{\omega} \phi \quad (3)$$

where

$$\underline{F}(\text{vac}) = \underline{\omega} \phi \quad (4)$$

is the force due to the vacuum. Here:

$$\phi = -\frac{nMG}{r} \quad (5)$$

is the gravitational potential and  $\underline{\omega}$  is a vector spin connection. From eqs. (1) and (3):

$$-\frac{nMG}{\gamma^3} \frac{\underline{r}}{r^3} = -nMG \frac{\underline{r}}{r^3} + \underline{\omega} \phi \quad (6)$$

so:

$$\underline{\omega} = \frac{\underline{r}}{r^2} \left( \frac{1}{\gamma^3} - 1 \right) \quad (7)$$

and

$$\omega = |\underline{\omega}| = \frac{1}{r} \left( \left( \frac{1}{\gamma^3} - 1 \right)^2 \right)^{1/2} \quad (8)$$

i.e.

$$\omega = \frac{1}{r} \left| \frac{1}{\gamma^3} - 1 \right| - (9)$$

Here  $| \cdot |$  denotes the modulus or positive value:

$$\left| \frac{1}{\gamma^3} - 1 \right| := \left( \left( \frac{1}{\gamma^3} - 1 \right)^2 \right)^{1/2} - (10)$$

So

$$\omega = \frac{1}{r} \left| \left( 1 - \frac{v^2}{c^2} \right)^{3/2} - 1 \right| - (11)$$

$$= \frac{1}{r} \left( 1 - \left( 1 - \frac{v^2}{c^2} \right)^{3/2} \right) - (12)$$

Note that

$$\omega \xrightarrow{v \rightarrow 0} 0 - (13)$$

and in this limit the Newton equation is reduced as:

$$\underline{F} = m\underline{g} = -\frac{mM_G}{r^3} \underline{r} - (14)$$

and the orbit is a conic section, for example an ellipse. Therefore orbital precession from the relativistic Newton equation is due to the spacetime curvature (7) and the vacuum force:

$$\underline{F}(\text{vac}) = \underline{\omega} \phi = -\frac{mM_G}{r} \underline{\omega} - (15)$$

From UFT too, the vacuum fluctuation due

1) To the spin comedia is:

$$\begin{aligned} \langle \underline{S}_r \cdot \underline{S}_r \rangle &= \frac{3}{2} r^3 \omega \\ &= \frac{3}{2} r^3 \left( 1 - \left( 1 - \frac{v^2}{c^2} \right)^{3/2} \right) \quad - (16) \end{aligned}$$

For small precessions:

$$v^2 = mG \left( \frac{2}{r} - \frac{1}{a} \right) \quad - (17)$$

which is the Newtonian orbital velocity of an object  $m$  orbiting an object  $M$  on an ellipse. Here  $a$  is the semi major axis:

$$a = \frac{d}{1 - \epsilon^2} \quad - (18)$$

here  $d$  is the half right distance and  $\epsilon$  is the eccentricity.

Therefore  $\langle \underline{S}_r \cdot \underline{S}_r \rangle$  can be worked out as any orbit, which is given in astronomy in terms of  $d$  and  $\epsilon$ .

The angular frequency  $\Omega_0$  of the precession which is given for LUT hold as:

$$\Omega_0^2 = \frac{2}{3} \frac{mG}{r^4} \langle \underline{S}_r \cdot \underline{S}_r \rangle^{1/2} = \frac{2}{3} \left( \frac{3}{2} \right)^{1/2} \frac{mG}{r^3} \left( 1 - \left( 1 - \frac{v^2}{c^2} \right)^{3/2} \right)^{1/2}$$

Therefore can also be worked out for any orbit.

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